

Collecting invariants of data structures

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Content

Collect the class invariants of various data structures.

Set aside all problems regarding the consistency of aggregate objects.

Motivation

Have a formal description of data structures.

Improve quality of automatically generated code.

How did we group the data structures?

Access

Dictionary
Stack
Queue
Deque

Storage

Linked-lists
Hash-tables
Trees

Example: Stack

```
deferred class STACK [G]
feature
  push (v: G)
    deferred
    ensure
      sequence.first = v
      sequence.but_first = (old sequence)
    end
  pop: G
    require
      sequence.count > 0
    deferred
    ensure
      Result = (old sequence).first
      sequence = (old sequence).but_first
    end
end
```

```
sequence: SEQUENCE [G]
invariant
  sequence.count ≥ 0
end
```

Example: Linked lists

```
class LINKED_LIST_CELL [G] feature
  key: G
  next: detachable like Current
invariant
  next  $\neq$  Current
end
```

```
class DOUBLY_LINKED_LIST_CELL [G] inherit LINKED_LIST_CELL [G] feature
  previous: detachable like Current
invariant
  previous  $\neq$  Current
  (next  $\neq$  Void)  $\Rightarrow$  next.previous = Current
  (previous  $\neq$  Void)  $\Rightarrow$  previous.next = Current
end
```

```
class CIRCULAR_LINKED_LIST_CELL [G] inherit DOUBLY_LINKED_LIST_CELL [G] feature
  cycle: SEQUENCE [like Current]
invariant
  cycle.has (Current)
  cycle.first = cycle.last
   $\forall i: 2 \mid .. \mid \text{cycle.count} \mid \text{cycle}[i - 1].\text{next} = \text{cycle}[i]$ 
end
```

Limitations

For any data structure, a static verifier might prefer a certain, distinct, but equivalent characterization of the chosen invariants.

All the class invariants must be complemented with specifications for the consistency of aggregate objects.

Thank you